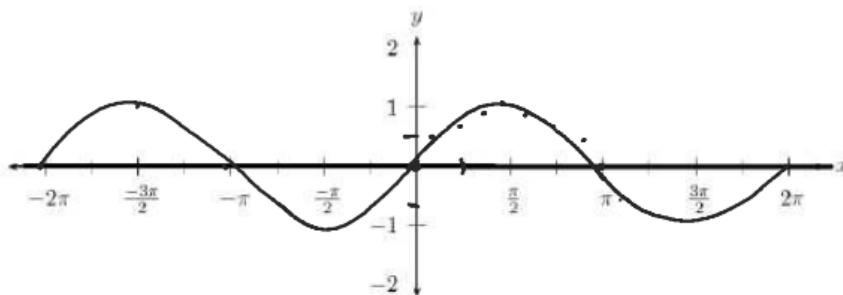


What you'll Learn About

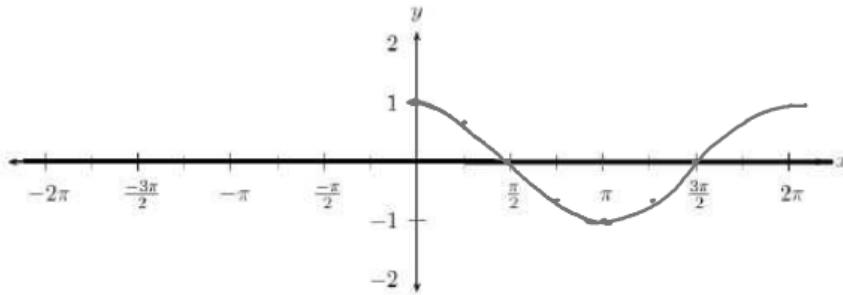
- The basic waves revisited/Sinusoids and Transformations
- Modeling

Cosine

x	y
0	0
$\frac{\pi}{6}$	$\frac{1}{2}$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2} \approx .707$
$\frac{\pi}{3}$	$\frac{\sqrt{3}}{2} \approx .866$
$\frac{\pi}{2}$	1
$\frac{2\pi}{3}$	$\frac{\sqrt{3}}{2} \approx .866$
$\frac{3\pi}{4}$	$\frac{\sqrt{2}}{2} \approx .707$
$\frac{5\pi}{6}$	$\frac{1}{2}$
π	0
$\frac{7\pi}{6}$	$-\frac{1}{2}$
$\frac{5\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$\frac{4\pi}{3}$	$-\frac{\sqrt{3}}{2} \approx -.866$
$\frac{3\pi}{2}$	-1
$\frac{2\pi}{3}$	$-\frac{1}{2}$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2} \approx .707$
$\frac{\pi}{6}$	$\frac{1}{2}$
0	0
$-\frac{\pi}{6}$	$-\frac{1}{2}$
$-\frac{\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{\pi}{3}$	$-\frac{\sqrt{3}}{2} \approx -.866$
$-\frac{\pi}{2}$	-1
$-\frac{2\pi}{3}$	$-\frac{1}{2}$
$-\frac{3\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{5\pi}{6}$	$-\frac{1}{2}$
$-\pi$	0
$-\frac{7\pi}{6}$	$-\frac{1}{2}$
$-\frac{5\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{4\pi}{3}$	$-\frac{\sqrt{3}}{2} \approx -.866$
$-\frac{3\pi}{2}$	-1
$-\frac{2\pi}{3}$	$-\frac{1}{2}$
$-\frac{\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{\pi}{6}$	$-\frac{1}{2}$
0	0

The graph of $y = \sin x$ 

x	y
0	1
$\frac{\pi}{6}$	$\frac{\sqrt{3}}{2} \approx .866$
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2} \approx .707$
$\frac{\pi}{3}$	$\frac{1}{2}$
$\frac{\pi}{2}$	0
$\frac{2\pi}{3}$	$-\frac{1}{2}$
$\frac{3\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$\frac{5\pi}{6}$	$-\frac{\sqrt{3}}{2} \approx -.866$
π	-1

The graph of $y = \cos x$ 

x	y
$-\pi$	$-\frac{\sqrt{3}}{2} \approx -.866$
$-\frac{4\pi}{3}$	$-\frac{1}{2}$
$-\frac{3\pi}{2}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{5\pi}{6}$	$-\frac{1}{2}$
$-\frac{\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$-\frac{\pi}{6}$	$-\frac{1}{2}$
0	0
$\frac{\pi}{6}$	$-\frac{1}{2}$
$\frac{\pi}{4}$	$-\frac{\sqrt{2}}{2} \approx -.707$
$\frac{3\pi}{4}$	$-\frac{1}{2}$
$\frac{5\pi}{6}$	$-\frac{\sqrt{3}}{2} \approx -.866$
π	-1

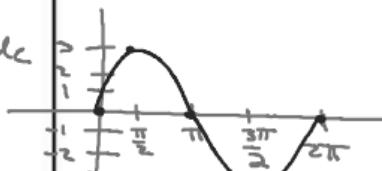
$$y = A \sin x$$

$$y = A \cos x$$

$|A| = \text{Amplitude}$

Find the amplitude of the function and use the language of transformations to describe how the graph of the function is related to the graph of $y = \sin x$

A) $y = 3 \sin x$



B) $y = \frac{3}{4} \sin x$

$$A = \frac{3}{4}$$

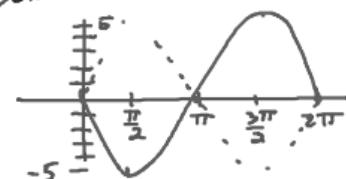
Vertical Compression
by a factor of $\frac{3}{4}$

Vertical Stretch
by a factor of 3

C) $y = 5 \sin x$

$$A = 5$$

Vert stretch
by a factor of 5
Reflect over
x-axis



$$y = A \sin Bx$$

$$y = A \cos Bx$$

$$\text{Period} = \frac{2\pi}{B}$$

$$\frac{2\pi}{\frac{4}{3}} \cdot \frac{4}{3} = \frac{8\pi}{3}$$

$$\frac{3}{4}$$

Find the period of the function and use the language of transformations to describe how the graph of the function is related to the graph of $y = \cos x$

A) $y = \cos(2x)$

$$\text{Per} = \frac{2\pi}{B} \\ = \frac{2\pi}{2} = \pi$$

B) $y = \cos \frac{x}{2}$

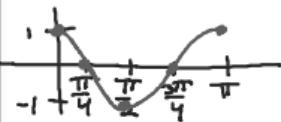
$$B = \frac{1}{2}$$

$$\text{Per} = \frac{2\pi}{B} \\ = \frac{2\pi}{\frac{1}{2}} \\ = 4\pi$$

C) $y = \cos \left(\frac{-3x}{4} \right)$

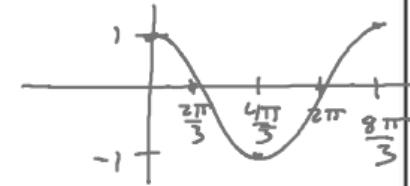
$$B = \frac{3}{4}$$

$$\text{Per} = \frac{2\pi}{B} \\ = \frac{2\pi}{\frac{3}{4}} \\ = \frac{8\pi}{3}$$



$B = \frac{1}{2}$

$$\text{Per} = \frac{2\pi}{B} \\ = \frac{2\pi}{\frac{1}{2}} \\ = 4\pi$$

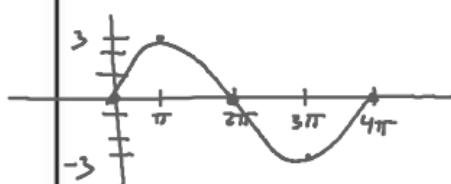


Graph 1 period of the function without using your calculator.

A) $y = 3 \sin \frac{x}{2}$

Amp = 3

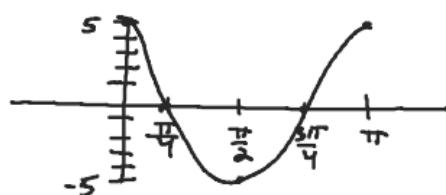
Per $\frac{2\pi}{\frac{1}{2}} = 4\pi$



$y = 5 \cos 2x$

Amp = 5

Per $\frac{2\pi}{2} = \pi$



Identify the maximum and minimum values and the zeros of the function in the interval $[-2\pi, 2\pi]$. Use your understanding of transformations, not your calculator.

A) $y = 4 \sin x$

B) $y = -2 \cos \frac{x}{3}$